

Find $\frac{dy}{dx} \Big|_{x=0}$ where $y = \frac{\sqrt{x^2+1} \cdot e^{\cos x} \cdot \cos^e x}{(1+x \sin x)^2 \cdot 2^{3^x}}$

$$\ln y = \ln \frac{\sqrt{x^2+1} \cdot e^{\cos x} \cdot \cos^e x}{(1+x \sin x)^2 \cdot 2^{3^x}}$$

$$y(0) = \frac{e}{2}$$

$$= \frac{1}{2} \ln(x^2+1) + \cos x + e \ln(\cos x) - 2 \ln(1+x \sin x) - 3^x \ln 2$$

$$\frac{y'}{y} = \frac{1}{2} \cdot \frac{2x}{x^2+1} - \sin x + e \cdot \frac{(-\sin x)}{\cos x} - 2 \cdot \frac{(\sin x + x \cos x)}{1+x \sin x} - 3^x \cdot \ln 3$$

$$y'(0) = y(0) \left[\frac{1}{2} \cdot 0 - 0 + e \cdot 0 - \frac{2 \cdot 0}{1+0} - 1 \cdot \ln 3 \cdot \ln 2 \right]$$

$$= \frac{1 \cdot e \cdot 1}{2} \cdot (-\ln 3 \cdot \ln 2)$$

$$= -\frac{e \cdot \ln 3 \cdot \ln 2}{2}$$