

# Chapter 5

## Some Discrete Probability Distributions

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# Section 5.1

## Introduction and Motivation

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# Section 5.2

## Binomial and Multinomial Distributions

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# Theorem 5.1



The mean and variance of the binomial distribution  $b(x; n, p)$  are  
$$\mu = np \text{ and } \sigma^2 = npq.$$

# Section 5.3

## Hypergeometric Distribution

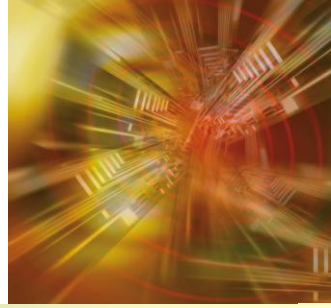
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# Theorem 5.2



The mean and variance of the hypergeometric distribution  $h(x; N, n, k)$  are

$$\mu = \frac{nk}{N} \text{ and } \sigma^2 = \frac{N-n}{N-1} \cdot n \cdot \frac{k}{N} \left(1 - \frac{k}{N}\right).$$

# Section 5.4

## Negative Binomial and Geometric Distributions

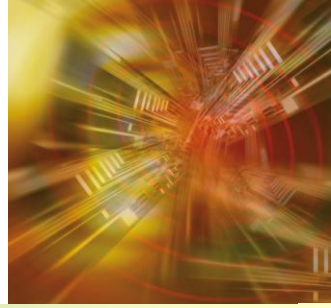
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# Theorem 5.3



The mean and variance of a random variable following the geometric distribution are

$$\mu = \frac{1}{p} \text{ and } \sigma^2 = \frac{1-p}{p^2}.$$



# Section 5.5

## Poisson Distribution and the Poisson Process

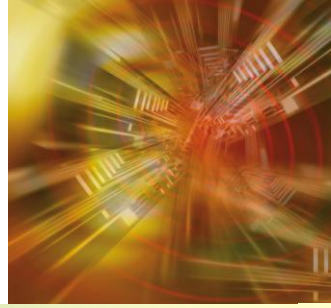
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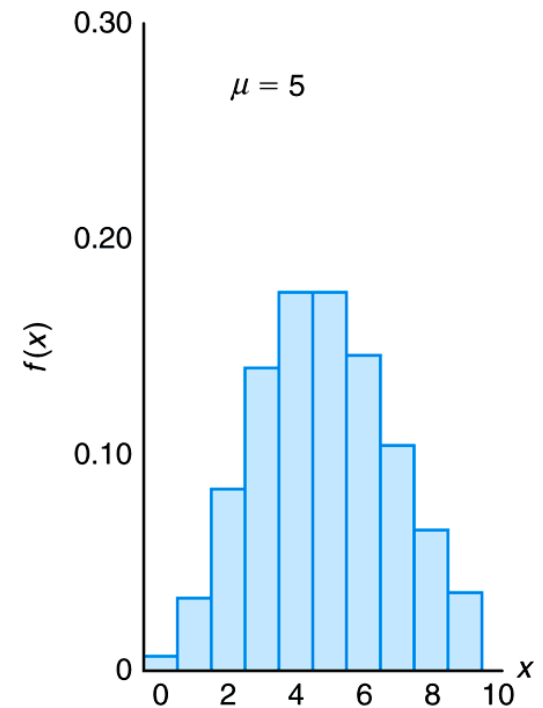
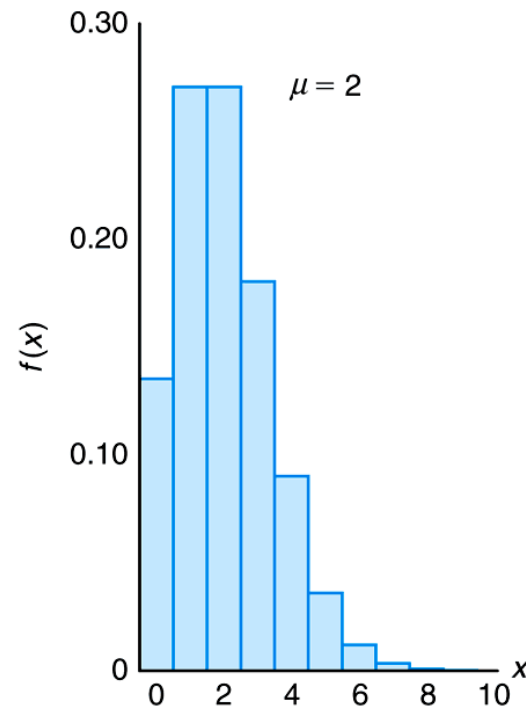
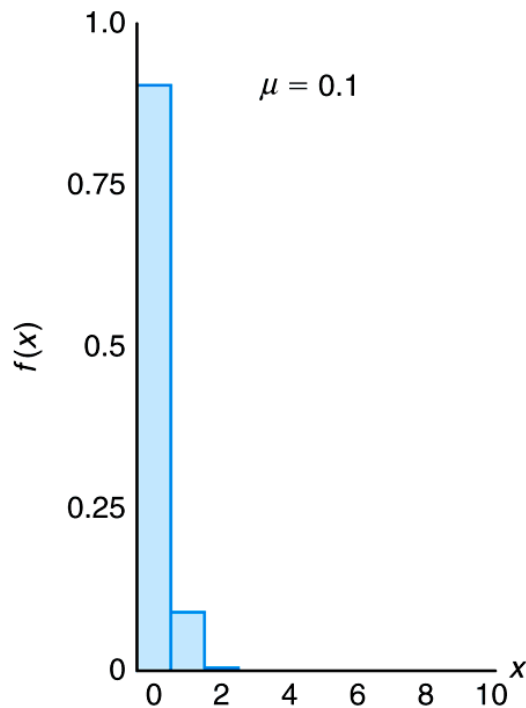
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# Theorem 5.4

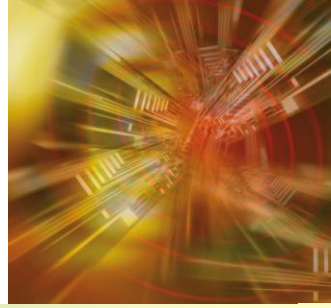


Both the mean and the variance of the Poisson distribution  $p(x; \lambda t)$  are  $\lambda t$ .

# Figure 5.1 Poisson density functions for different means



# Theorem 5.5



Let  $X$  be a binomial random variable with probability distribution  $b(x; n, p)$ . When  $n \rightarrow \infty$ ,  $p \rightarrow 0$ , and  $np \xrightarrow{n \rightarrow \infty} \mu$  remains constant,

$$b(x; n, p) \xrightarrow{n \rightarrow \infty} p(x; \mu).$$

# Section 5.5

Potential  
Misconceptions  
and Hazards;  
Relationship to  
Material in Other  
Chapters

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