On The Trace Formula for a Differential Operator of Second Order with Unbounded Operator Coefficients

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We investigate the spectrum of a differential operator of second order with unbounded operator coefficients and two terms and we calculate the trace of this operator.

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