

Şekil 2. Çeyrek taşıt modeli

### Lagrange Denklemi

$$\frac{d}{dt} \left( \frac{\partial E_k}{\partial \dot{q}_i} \right) - \frac{\partial E_k}{\partial q_i} + \frac{\partial E_p}{\partial q_i} + \frac{\partial E_c}{\partial \dot{q}_i} = Q_i$$

$q_i$ : Genelleştirilmiş Koordinat

$E_k$ : Kinetik Enerji

$E_p$ : Potansiyel Enerji

$E_c$ : Sönüm Enerjisi Enerji

$Q_i$ : Genelleştirilmiş Kuvvet

$$E_k = \frac{1}{2} m_s (\dot{z}_s)^2 + \frac{1}{2} m_u (\dot{z}_u)^2$$

$$E_p = \frac{1}{2} k_s (z_s - z_u)^2 + \frac{1}{2} k_t (z_u - z_r)^2$$

$$E_c = \frac{1}{2} c_s (\dot{z}_s - \dot{z}_u)^2 + \frac{1}{2} c_t (\dot{z}_u - \dot{z}_r)^2$$

$z_s$  Genelleştirilmiş Koordinatı İçin

$$\frac{d}{dt} \left( \frac{\partial E_k}{\partial \dot{z}_s} \right) = \frac{d}{dt} \left( \frac{1}{2} (m_s \dot{z}_s) \right) = \frac{d}{dt} (m_s \dot{z}_s) = m_s \ddot{z}_s$$

$$\frac{\partial E_k}{\partial z_s} = 0$$

$$\frac{\partial E_p}{\partial z_s} = \frac{1}{2} 2k_s (z_s - z_u) = k_s (z_s - z_u)$$

$$\frac{\partial E_c}{\partial \dot{z}_s} = \frac{1}{2} 2c_s (\dot{z}_s - \dot{z}_u) = c_s (\dot{z}_s - \dot{z}_u)$$

$$Q_{z_s} = 0$$

$$m_s \ddot{z}_s + k_s (z_s - z_u) + c_s (\dot{z}_s - \dot{z}_u) = 0$$

$z_u$  Genelleştirilmiş Koordinatı İçin

$$\frac{d}{dt} \left( \frac{\partial E_k}{\partial \dot{z}_u} \right) = \frac{d}{dt} \left( \frac{1}{2} (m_u \dot{z}_u) \right) = \frac{d}{dt} (m_u \dot{z}_u) = m_u \ddot{z}_u$$

$$\frac{\partial E_k}{\partial z_u} = 0$$

$$\frac{\partial E_p}{\partial z_u} = -\frac{1}{2} 2k_s (z_s - z_u) + \frac{1}{2} 2k_t (z_u - z_r) = -k_s (z_s - z_u) + k_t (z_u - z_r)$$

$$\frac{\partial E_c}{\partial \dot{z}_u} = -\frac{1}{2} 2c_s (\dot{z}_s - \dot{z}_u) + \frac{1}{2} 2c_t (\dot{z}_u - \dot{z}_r) = -c_s (\dot{z}_s - \dot{z}_u) + c_t (\dot{z}_u - \dot{z}_r)$$

$$Q_{z_u} = 0$$

$$m_u \ddot{z}_u + -k_s (z_s - z_u) + k_t (z_u - z_r) - c_s (\dot{z}_s - \dot{z}_u) + c_t (\dot{z}_u - \dot{z}_r) = 0$$

$$m_s \ddot{z}_s + k_s(z_s - z_u) + c_s(\dot{z}_s - \dot{z}_u) = 0$$

$$m_u \ddot{z}_u + -k_s(z_s - z_u) + k_t(z_u - z_r) - c_s(\dot{z}_s - \dot{z}_u) + c_t(\dot{z}_u - \dot{z}_r) = 0$$

$$\begin{bmatrix} m_s & 0 \\ 0 & m_u \end{bmatrix} \begin{bmatrix} \ddot{z}_s \\ \ddot{z}_u \end{bmatrix} + \begin{bmatrix} c_s & -c_s \\ -c_s & c_s + c_t \end{bmatrix} \begin{bmatrix} \dot{z}_s \\ \dot{z}_u \end{bmatrix} + \begin{bmatrix} k_s & -k_s \\ -k_s & k_s + k_t \end{bmatrix} \begin{bmatrix} z_s \\ z_u \end{bmatrix} = \begin{bmatrix} 0 \\ c_t \end{bmatrix} \dot{z}_r + \begin{bmatrix} 0 \\ k_t \end{bmatrix} z_r$$

$$m_s \ddot{z}_s + k_s(z_s - z_u) + c_s(\dot{z}_s - \dot{z}_u) = 0$$

$$m_u \ddot{z}_u = -k_s(z_s - z_u) + k_t(z_u - z_r) - c_s(\dot{z}_s - \dot{z}_u) + c_t(\dot{z}_u - \dot{z}_r) = 0$$

$$\ddot{z}_s = \left(\frac{-1}{m_s}\right) (k_s(z_s - z_u) + c_s(\dot{z}_s - \dot{z}_u))$$

$$\ddot{z}_u = \left(\frac{-1}{m_u}\right) (-k_s(z_s - z_u) + k_t(z_u - z_r) - c_s(\dot{z}_s - \dot{z}_u) + c_t(\dot{z}_u - \dot{z}_r))$$

$$z_s \rightarrow u(1)$$

$$\dot{z}_s \rightarrow u(2)$$

$$z_u \rightarrow u(3)$$

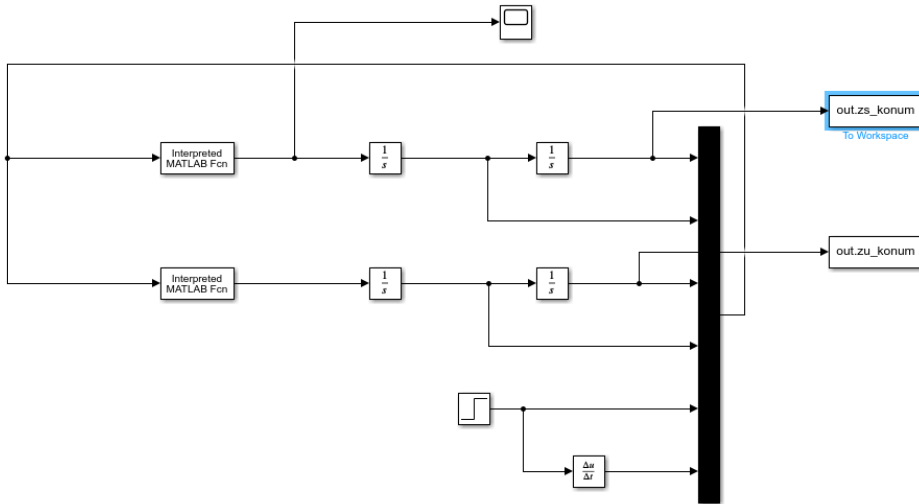
$$\dot{z}_u \rightarrow u(4)$$

$$z_r \rightarrow u(5)$$

$$\dot{z}_r \rightarrow u(6)$$

$$(-1/ms)*(ks*(u(1)-u(3))+cs*(u(2)-u(4)))$$

$$(-1/mu)*(-ks*(u(1)-u(3))+kt*(u(3)-u(5))-cs*(u(2)-u(4))+ct*(u(4)-u(6)))$$



**%Parametreler:**

```
ms=290;      % kg    --> % AnaGövde Kütlesi
mu=40;       % kg    --> % Süspansiyon Kütlesi
ks=13000;    % N/m   --> % Süspansiyon Yay Katsayısı
kt=220000;   % N/m   --> % Tekerlek Yay katsayısı
cs=1000;     % Ns/m  --> % Süspansiyon Sönümü Katsayısı
ct=0;        % Ns/m  --> % Tekerlek Sönümü Katsayısı
```

```
sim('proje1')
```

```
plot(out.zs_konum)
```